

# Reasoning Logically with "if" and "then"

$$\begin{array}{l} P \rightarrow Q \\ P \\ \hline Q \end{array}$$

if today is Tues, then it is a weekday  
today is Tues.

Therefore: it is a weekday

$$\begin{array}{l} P \rightarrow Q \\ Q \\ \hline ??? \end{array}$$

if today is Tues, then it is a weekday  
it is a weekday.

I do not know the day based on this

$$\begin{array}{l} P \rightarrow Q \\ \neg P \\ \hline ??? \end{array}$$

if today is tues, then it is a weekday  
today is not tues.

I do not know if it is a weekday  
based on this

$$\begin{array}{l} P \rightarrow Q \\ \neg Q \\ \hline \neg P \end{array}$$

if today is tues, then it is a weekday  
it is NOT a weekday.

Therefore it cannot be tues.